

4762

Mark Scheme

June 2012

Question			Answer	Marks	Guidance
1	(a)	(i)	KE change: $\frac{1}{2} \times 0.6 \times (7.5^2 - 5.5^2)$ = 7.8 J GPE change: $0.6 \times 9.8 \times 1.5 = 8.82$ J	M1 A1 B1 [3]	Difference of two KE terms Allow -8.82J
1	(a)	(ii)	W is work done against resistance $7.8 = 8.82 - W$ so $W = 1.02$ J	M1 A1 [2]	W-E all terms. Allow sign errors FT (i) only. Also FT only if mod (their KE) < mod (their PE) -1.02 gets M1A0; 16.62 gets M1A0
1	(a)	(iii)	Average resistance is F so $F \times 1.5 = 1.02$ so $F = 0.68$ Power is 0.68×5.5 = 3.74 so 3.74 W	M1 A1 M1 A1 [4]	Use of $WD = Fs$ OR find $a = 8.667$ and use $F = 0.6g - 0.6 \times 8.667$ May be implied. FT (ii) Use of $P = Fv$ any calculated F cao
1	(b)	(i)	$R = mg \cos 40$ $F_{\max} = mg \sin 40$ $F_{\max} = \mu R$ so $\mu = \frac{mg \sin 40}{mg \cos 40} = \tan 40$	B1 B1 M1 E1 [4]	Seen or implied Seen or implied Use of $F = \mu R$: substitute F and R This is the minimum amount of working needed to earn the E1 Must see explicit evidence of method Note: g omitted, treat as MR
1	(b)	(ii)	EITHER $\tan 40 \times 0.8 \times 9.8 \times \cos 20$ $\times 3 (= 18.545)$ (+) 0.8×9.8 $\times 3 \sin 20 (= 8.044)$ = 26.5897... so 26.6 J (3 s.f.)	B1 M1 B1 M1 A1	Use of $F_{\max} = \mu R$ with $\tan 40$ and $\cos 20$ Use of $WD = Fs$ NOTE: This mark may be awarded here or for use in PE term Use of mgh Allow $\sin \leftrightarrow \cos$ interchange Two relevant terms added Cao Allow 26.7 Allow 27 Omission of g can get B0M1B1M1A0

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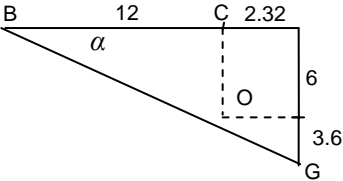
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		OR $\tan 40 \times 0.8 \times 9.8 \times \cos 20 (= 6.182)$ $(+) 0.8 \times 9.8 \times \sin 20 (= 2.68)$ $(= 8.8632444\dots)$ WD is $3 \times 8.8632444\dots$ $= 26.5897\dots$ so 26.6 J (3 s.f.)	B1 B1 M1 M1 A1 [5]	Use of $F_{\max} = \mu R$ with $\tan 40$ and $\cos 20$ Allow $\sin \leftrightarrow \cos$ interchange Two relevant forces added Use of $WD = Fs$ (for at least one of forces) cao Omission of g can get B0B1M1M1A0
2	(i)	a.c. moments about B $10T_C - 15 \times 2 = 0$ so $T_C = 3$. Tension at C is 3 N $\uparrow T_C + T_B - 15 = 0$ so $T_B = 12$. Tension at B is 12 N	M1 A1 M1 F1 [4]	Moments with all forces present, no extra forces. May take moments again
2	(ii)	a.c. moments about A $25T \sin 30 - 15 \times 17 = 0$ so $T = 20.4$ At A Let force \uparrow be Y N $\uparrow Y + T \sin 30 - 15 = 0$ so $Y = 4.8$ $\rightarrow X = T \cos 30 = 17.6669\dots$ N $\sqrt{4.8^2 + (T \cos 30)^2}$ $= 18.3073755\dots$ so 18.3 N (3 s.f.)	M1 A1 B1 B1 M1 A1 [6]	Attempt at moments with resolution; allow $\cos \leftrightarrow \sin$ error. All forces present, no extra forces cao FT (can take moments about C) FT Need not be evaluated cao
2	(iii)	Let force be P . a.c. moments about D. $8 \times 15 - 12 \times P = 0$ so $P = 10$ on point of tipping Using $F_{\max} = \mu R$ on point of slipping with $R = 15$ gives $F_{\max} = 0.65 \times 15 = 9.75$ so slips first	M1 A1 M1 B1 A1 E1 [6]	Moments about D with all forces present, no extra forces cao cao cao and WWW

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3	(a)	(i)	$300 \begin{pmatrix} \bar{x} \\ \bar{y} \end{pmatrix} = 72 \begin{pmatrix} -6 \\ 3 \end{pmatrix} + 192 \begin{pmatrix} 4 \\ -6 \end{pmatrix} + 36 \begin{pmatrix} 10 \\ -4 \end{pmatrix}$ $\begin{pmatrix} \bar{x} \\ \bar{y} \end{pmatrix} = \begin{pmatrix} 696 \\ -1080 \end{pmatrix}$ so $\bar{x} = 2.32$ $\bar{y} = -3.6$	B1 M1 B1 A1 A1 [5]	Correctly identifying the position of the c.m of triangle EFH (10, -4) A systematic method for at least 1 cpt <i>Either all x or all y values correct or 2 vector terms correct or allow one common error in both components, e.g. one wrong mass, misunderstanding of c.m. of triangle</i> Allow FT for either if only error is common to both
3	(a)	(ii)	 <p>centre of mass is at G</p> $\tan \alpha = \frac{9.6}{14.32}$ so $\alpha = 33.8376\dots$ so 33.8° (3 s.f.)	M1* B1 M1dep* A1 [4]	Identifying correct angle. May be implied At least 1 relevant distance found. FT (i) Use of $\arctan \frac{9.6}{14.32}$ or $\arctan \frac{14.32}{9.6}$ o.e. cao or $180^\circ - 33.8^\circ$
3	(b)	(i)	Marking given tension and thrust Marking all other forces internal to rods acting on A, B and C (as T or C)	B1 B1 [2]	Each labelled with magnitude and correct direction Need ALL forces at A, B and C. Need pairs of arrows on AB, AC and BC

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3	(b) (ii)	Equilibrium at A \uparrow $T_{AB} \cos 30 - 18 = 0$ $T_{AB} = 12\sqrt{3}$. Force in AB: $12\sqrt{3}$ N (T) A \leftarrow $T_{AC} + T_{AB} \cos 60 + 5 = 0$ $T_{AC} = -(5 + 6\sqrt{3})$. Force in AC: $(5 + 6\sqrt{3})$ N (C) At B in direction AB $T_{BR} \cos 60 - T_{AB} = 0$ so $T_{BR} = 24\sqrt{3}$ At B in direction BC $T_{BC} - T_{BR} \cos 30 = 0$ $T_{BC} = 36$. Force in BC: 36 N (T)	M1 A1 M1 F1 M1 F1 A1 [7]	Equilibrium at one pin-joint 20.8 Sign consistent with tension on their diagram -15.39 FT their T_{AB} Allow FT Other methods are possible, but award this M1 only for a complete method that would lead to T_{BC} cao WWW T/C all correct
4	(i)	$26t = 3 \times 13$ $t = 1.5$ so 1.5 s	M1 A1 [2]	Use of $Ft = m(v - u)$ or N2L to find a ($= 26/3$) and use $v = u + at$ cao
4	(ii)	PCLM $10 \times 0 + 3 \times 13 = 10v_Q + 3v_P$ $39 = 10v_Q + 3v_P$ NEL $\frac{v_Q - v_P}{0 - 13} = -e$ $v_Q - v_P = 13e$ $v_Q = 3(1 + e)$ $v_P = 3 - 10e$	M1 A1 M1 A1 M1 B1 E1 [7]	Use of PCLM Any form Use of NEL. Allow sign errors but not inversion Any form Eliminating one of v_Q or v_P OR allow substitution of given result in one equation and check both answers in other equation cao; aef Properly shown

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4	(iii)	Need $v_p < 0$ so $3 - 10e < 0$ Hence $\frac{3}{10} < e \leq 1$	M1 A1 [2]	Accept \leq cao (Allow $e \leq 1$ omitted) Correct answer www gets 2/2
4	(iv)	When $e > \frac{3}{10}$, its speed is $10e - 3$ We require $(10e - 3) > 3(1 + e)$ so $7e > 6$ and so $\frac{6}{7} < e \leq 1$	M1 M1 A1 A1 [4]	FT their v_Q SC1 for $(3 - 10e) > \pm 3(1 + e)$ FT their v_Q cao. Allow $e > \frac{6}{7}$ (0.857) Correct answer www gets 4/4
4	(v)	Either $v_Q = 4.5$ and $v_p = -2$ When they collide the speed of Q is -4.5 and of P is 2 PCLM $10 \times -4.5 + 3 \times 2 = 13V$ so $V = -3$ and velocity is -3 m s^{-1}	M1 M1 M1 A1 [4]	Substitute $e = 0.5$; FT their v_Q Change signs of their velocities Use of PCLM Allow sign errors cao; OR 3 m s^{-1} to the right or use argument about final LM is $-ve$ of original LM
		Or $10(-3(1+e)) + 3(10e-3) = 13V$ $-39 = 13V$ so $V = -3$ and velocity is -3 m s^{-1}	M1 M1 M1 A1 [4]	Use of PCLM; Allow sign errors ; FT their v_Q Change signs of their velocities Simplify cao; OR 3 m s^{-1} to the right
4	(vi)	$3(-3-2) = -15 \text{ N s}$	B1 [1]	FT $3(\text{their}(v) - 2)$ Using $10(-3 + 4.5) = 15$ gets B0 until it leads to correct answer